

Design and Analysis of Leaf Spring

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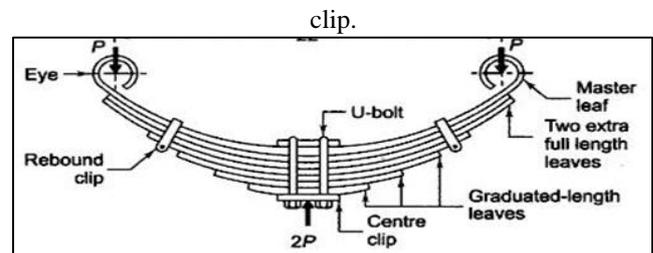
Abstract— A multi-leaf spring is one of the important components of automobile suspension system. Leaves are basically a series of flat plates, usually of elliptical shape. Generally, a multi-leaf spring used in automobile suspension, consists of 2 types of leaves i.e. graduated-length leaves and full-length spring. The current work is an attempt to estimate the magnitude of bending stresses in the above mentioned leaves for a semi-elliptic multi-leaf spring made of steel. A lot of work has been carried out in the context of leaf spring considering its material and a important progress has been observed in the field of weight reduction, improvement of load carrying capacity when he replace the material of the spring by any advanced material like composites as E-glass/epoxy, carbon/epoxy etc. Finally referring to the grades obtained in the studies, the present work proposes a new idea regarding the construction of multi-leaf spring based on practical applications. Dimensions of the multi-leaf spring are taken from practical understanding and calculate dimension manually from standard chart of automobile spring. The leaf spring has modelled in CATIA and the same examined under similar environments using ANSYS (Workbench 16.0).

Key words: Leaf Spring

I. INTRODUCTION

A spring is an elastic mechanical element which undergoes deflection for the solicitation of any load and intends to regain its original shape subject upon the magnitude of the applied load. The main applications of spring is include its use as a shock and vibration gain and storing potential energy by its deflection during the solicitation of load. A multi-leaf spring or coated spring is a important component in automobile system. It is one of the oldest suspension components too and still today it is extensively used in all the heavy and light duty commercial vehicles, railway wagons and usually in the rear suspension of passenger vehicles. It differs from the conventional helical spring in a way that it can be guided along a definite path and it deflects under the application of load while acting as a structural member. This concept is working during the analysis of bending stresses in altered leaves by consideration of cantilever beam. The present work makes an attempt to validate the above concept by performing static structural analysis using ANSYS software for the evaluation of maximum bending stress and subsequently bending stresses in different leaves, which in all concept the entire spring.

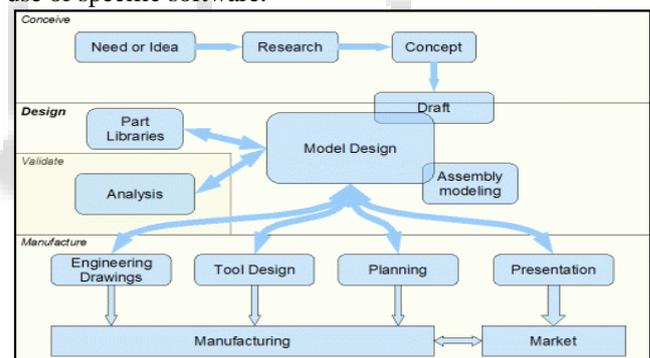
In its construction the leaf spring consists of a series of flat plates or leaves, usually of semi-elliptic shape, which are held together with the help of U-bolts and centre



II. COMPUTER AIDED ENGINEERING (CAE)

A. CAD (Computer Aided Designing)

Computer-aided design (CAD) is the use of computer systems to aid in the making, alteration, examination, or optimization of a design. CAD software is used to develop the productivity of the designer, increase the quality of design, and to create a catalogue for manufacturing. CAD output is often in the form of electronic files for copy, machining, or other manufacturing processes. Each phase requires exact knowledge and abilities and often requires the use of specific software.



B. Need or Idea

Usually, the design process starts with a defined need. The need can be defined by market research, by the requirements of a larger body of work (for example airplane part). Sometimes, but more rarely than you may think, the design process is begun with a new idea or invention. At any rate, a needs analysis should precede any decision to undertake a project. This includes defining the need in a highly detailed way, in writing. This is similar to the requirements specification process in software engineering.

C. Research

Specialists to research available solutions afore beginning their work. There is no need to "reinvent the wheel". You should study existing solutions and concepts, evaluating their weaknesses and strengths. Your research should also cover available parts that you can use as a part of your design. It is obvious, that Internet and search engines like Google are very helpful for this task. There are also many libraries of standardized parts which you can import into your project.

D. Concept

Based on your research, start with a high level concept. You should specify the main principles and major parts. For example, you can consider Diesel or Sterling engines for stationary electric generators.

E. Draft

You can choose to create a draft by pen and paper. Some prefer to use simple vector graphics programs, others even simple CAD (for example Smart Sketch), yet others prefer to start directly in their main CAD system.

F. Model Design

2D and 3D modelling in CAD. The designer creates a model with details, and this is the key part of the design process, and often the most time consuming. This will be described in greater detail in further lessons. asaceva

G. Part Libraries

Standard parts, or parts created by other team members, can be used in your model (you don't have to reinvent the wheel). Files representing a part can be downloaded from the Internet or local networks. They are also distributed on CD ROMs or together with CAD as an extension (library). By putting these predefined parts into your project, you ensure that they are correct and save a lot of time and effort. When working on a large project, this becomes a requirement to ensure the parts operate together, swap out equivalent parts, and coordinate distributed teams' work. This was, a standard part can be inserted into the project by one team member.

H. Assembly modelling

Parts are assembled into a machine or mechanism. Parts are put together using mating conditions such as alignment of the axis of two holes. More about how to do this in further lessons. Cad is used in industries.

I. Engineering Drawings

From your 3D models, you generate a set of engineering drawings for manufacturing. These drawings are then distributed to the departments and individuals responsible for producing that work. Also, these drawings must be tolerance for proper manufacturing.

J. About CATIA V5

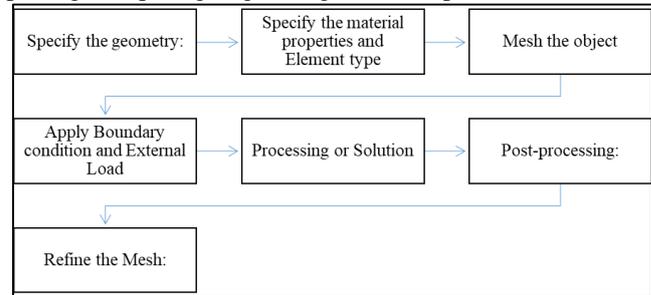
CATIA (an acronym of computer aided three-dimensional interactive application) is a multi-platform software suite for computer-aided design (CAD), computer-aided manufacturing (CAM), computer-aided engineering (CAE), PLM and 3D, developed by the French company Dassault Systems..

K. Finite Element Analysis (FEA)

FEA is a numerical method. It is very commonly used in finding the solution of many problems in engineering. The problem includes deigning of the shaft, truss bridge, buildings heating and ventilation, fluid flow, electric and magnetic field and so on. The main advantage of using finite element analysis is that many designs can be tried out for their validity, safety and integrity using the computer, even before the first prototype is built. Finite element analysis uses the idea of dividing the large body in to small parts called

elements, connected at predefine points called as nodes. Element behavior is approximated in terms of the nodal variables called degrees of freedom. Procedure for FE Analysis

There are a number of steps in the solution procedure using finite element method. All finite element packages require going through these step.



III. MATHEMATICAL FORMULATION

For the purpose of analysis, the leaves are divided in two groups as master leaf along with graduated length leaves forming one group and the extra full-length leaves forming the other group.

Let,

n_f = number of extra full-length leaves,

n_g = number of graduated-length leaves including the master leaf,

$n = n_f + n_g$ = Total number of leaves present in the multi-leaf spring,

b = width of each leaf (mm),

t = thickness of each leaf (mm),

L = half the length of the semi-elliptic spring or the length of the cantilever (mm),

P = force applied at the end of the spring (N),

P_f = portion of P taken by the extra full-length leaves (N),

P_g = portion of P taken by the graduated-length leaves (N),

So,

$$P = P_f + P_g$$

Now, from practical considerations for an automobile leaf spring, that is of semi-elliptical shape usually, for a length of $2L$ and a load of $2P$ acting at the center, the entire beam can be considered as a double cantilever. If the leaves are cut into two equal halves in longitudinal plane and then combined accordingly, to form almost a triangular plate then,

The maximum bending stress is given by

$$(S_b)_{\max} = 6P.L/n.b.t^2$$

The bending stress in the graduated-length leaves is given by

$$(S_b)_g = 12P.L / (3.n_f + 2.n_g).b.t^2$$

The bending stress in the extra full-length leaves is given by

$$(s_b)_f = 18P.L / (3.n_f + 2.n_g).b.t^2$$

It is to be noted that, the maximum bending stress occurs at the supports for such a plate. The above relations hold good for the leaves (or plates), having uniform cross-section. Also, it is seen that the bending stresses in extra full-length leaves are 50% more than that of the graduated length leaves

$$\text{i.e. } (s_b)_f = 1.5(s_b)_g$$

Calculation of length of different leaves:

For the calculation of length of different leaves, following relations were used and subsequently, the results were implemented while modeling the multi-leaf spring in CATIA V5R18 software.

- Length of the smallest leaf = 1*Effective length/ (n-1) + Ineffective length
- Length of the next leaf = 2*Effective length/ (n-1) + Ineffective length
- Similarly, Length of the (n-1)th leaf = (n-1)*Effective length/ (n-1) + Ineffective length
- Length of master leaf = 2.L+ 2.P.(d+t)
- Ineffective length = Distance between the centres of U-bolts = 1
- Effective length = 2.L – 2.l/3 and
- d = inside diameter of eye.

IV. DESIGN SPECIFICATION

Here Weight and initial measurements of four wheeler "TATA ACE" Light commercial vehicle is taken.

Weight of vehicle= 1200kg

Maximum load carrying capacity= 1000 kg

Total weight= 1200+ 1000 = 2200 kg

Taking factor of safety (FS) = 2

Acceleration due to gravity (g) = 9.81m/s²

Therefore;

Total Weight = 2200×9.81 = 21582N

Since the vehicle is 4-wheeler, a single leaf spring corresponding to one of the wheels takes up one 4th of the total weight.

21582/4 = 5395.5 N

But 2F = 5395.5 N,

F = 2697.75 N

Span length,

2L = 1072 mm,

L= 536mm.

Now the Max Bending stress of a leaf spring is given by the formula

$$\sigma = \frac{6 \times f \times l}{n \times b \times t^2}$$

$$\sigma = \frac{6 \times 2697.75 \times 536}{3 \times 60 \times 8^2}$$

$$\sigma = 753.12\text{N/mm}^2$$

The Total Deflection of the leaf spring is given by

$$\delta = \frac{6 \times f \times l^3}{E \times n \times b \times t^3}$$

$$\delta = \frac{6 \times 2697.75 \times 536^3}{2.1 \times 10^5 \times 3 \times 60 \times 8^3}$$

$$\delta = 128.79\text{mm}$$

Measured data of the above stated light weight four wheeler vehicle.

Straight length of the parabolic leaf spring (L) =1072mm

The ratio of camber length of parabolic leaf spring

C/L = 0.089

C = 0.089 × 1072

C = 95.4 mm

Since the leaf spring is fixed with the axle at its centre, only half of it is considered for analysis purpose. Since analyzing half of the leaf spring is enough, half of the applied force would have been taken, but here we took as it is to account over loadings of the vehicle and flexures of the leaf spring.

Hence,

$$L/2= 536\text{mm}$$

$$F=2697.75\text{N} \quad t=? \quad b=?$$

Calculation for "t" and "b" dimensions which are capable of withstanding the loading behaviour of the conventional and composite parabolic leaf spring is the result of this design. From equation of strength of material we have, now the Maximum Bending stress of a leaf spring is given by the formula,

Bending Stress,

$$\sigma = \frac{6 \times f \times l}{n \times b \times t^2}$$

The Total Deflection of the leaf spring is given by

$$\delta = \frac{6 \times f \times l^3}{E \times n \times b \times t^3}$$

Solving these two equations the thickness and width of the parabolic leaf spring can be, formulated, respectively, as follows;

$$\sigma = \frac{6 \times 2697.75 \times 536}{3 \times b \times 8^2}$$

$$753.12 = \frac{6 \times 2697.75 \times 536}{3 \times b \times 8^2}$$

$$b=60\text{mm}$$

The Total Deflection of the leaf spring is given by

$$128.79 = \frac{6 \times 2697.75 \times 536^3}{2.1 \times 10^5 \times 3 \times 60 \times t^3}$$

$$t=8\text{mm}$$

The objective of the present course of study includes, determination of maximum bending stress for three different loading conditions and to establish the relationship for the magnitude of bending stresses existing in the graduated-length leaves and extra full-length leaves (i.e. $(\sigma_b) = 1.5(\sigma_b)g$), with the following dimensional specifications, Table 1 Specification of multi-leaf spring Parameters Value Notation Total length of the semi-elliptic spring (distance between two eyes) 1243 mm 2L width of each leaf 100 mm b thickness of each leaf 14 mm t number of extra full-length leaves 2 n number of graduated-length leaves including the master leaf 8 no Total number of leaves present in the multi-leaf spring 10 n Load acting at the center of the spring 15000 N, 10000 N, 5000 N 2P The dimensions are taken from practical understanding and the standards available in the market. Structural steel was considered as the leaf material with an

Elastic modulus E = 2.1*10⁵ MPa,

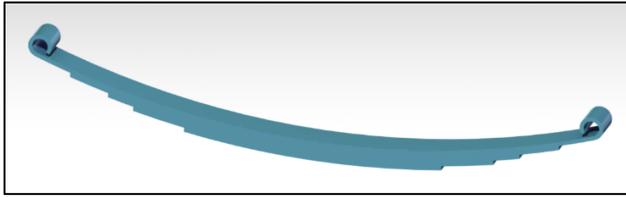
Tensile yield strength S_{yt} = 250 MPa

And

Poisson's ratio=0.3

While performing the analysis in ANSYS (Workbench 16.0) software.

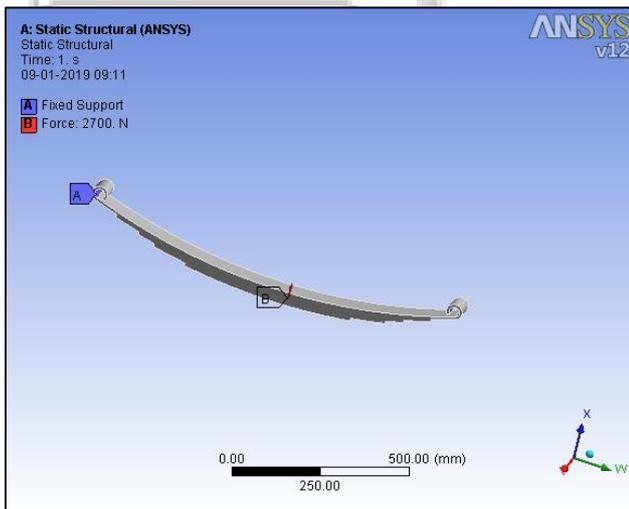
V. PROPOSED DESIGN



A. Static Analysis

The objective of this analysis is to investigate the stresses in the multi-leaf spring within the desirable limits to obtain a practical validation for the theoretical results. After geometric modeling in CATIA V5R18 software the spring is subjected to static analysis, performed in ANSYS (Workbench 16.0) software. The computer compatible mathematical description of the geometry of the object is called geometric modeling. CATIA is basically CAD (computer-aided design) software that allows the mathematical description of the object to be displayed and manipulated as the image on the monitor of the computer [7], whereas, ANSYS is an engineering simulation software that predicts with confidence about the performance of the product under the real-world environments incorporating all the existing physical phenomena. The layout of static analysis involves meshing, boundary conditions and loading.

B. Boundary Condition:

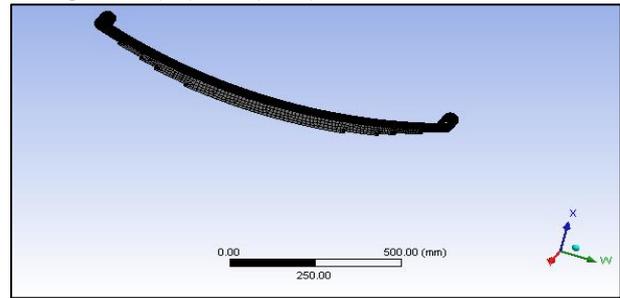


As shown in geometry is fixed at eye and force applied at bottom face

C. Meshing

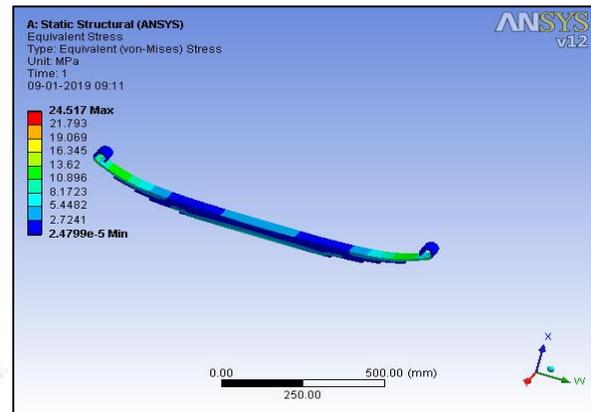
Meshing is basically the division of the entire model into small elements. In order to maintain the shape, it is convenient to select the free mesh, as the geometry of leaf spring contains sharp curves. Element size of 20 mm with medium smoothing was considered for mesh generation. Minimum edge length of the elements was 14 mm. Within the solution domain under the Adaptive Mesh Refinement segment, Max. Refinement Loops was taken as 3 and Refinement Depth as 2. For the convergence plot, the maximum allowable change was considered as 4%. All the 44 faces were selected for mesh generation and total number of nodes and elements were observed as 13423 and 7358 respectively. Figure 1 shows the meshed model of multi-leaf

spring. Load 2P (newton) 15000 10000 5000 Maximum Bending stress (σ)max (MPa) 142.691 95.127 47.563



Nodes	2087
Element	10870

D. Equivalent Stresses:



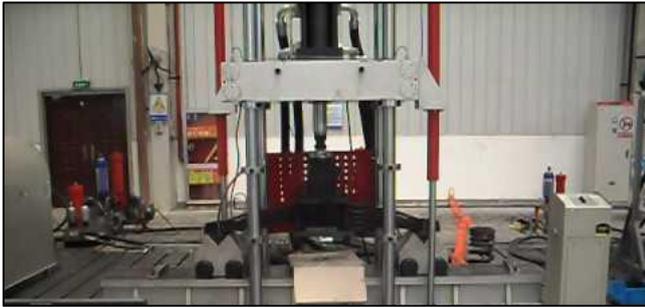
Load (Newton)	Von-mises Stress N/mm ²	Bending Stress N/mm ²	Deflection mm
1000	139.628	279.6	4.77
2000	282.615	558.2	9.54
3000	426.152	837.3	14.322
4000	568.83	1116.4	19.09
5000	712.642	1395.5	23.87
6000	852.345	1674.6	28.54
7000	993.515	1953.7	33.4
8000	1136.106	2332.5	38.192
9000	1277.672	2511.9	42.96
10000	1420.076	2791.6	47.74
11000	1458.076	3070.1	52.514
12000	1602.463	3349.2	57.28
13000	1746.091	3628.3	62.08
14000	1891.599	3907.4	66.83
15000	2037.106	41865	71.60

It is seen that at load 12000 N, it crosses the yield stress (yield stress is 1680 N/mm²). By considering the factor of safety 1.5 to 2, it is obvious that the allowable design stress is 840 to 1120 N/mm². So the corresponding loads are 6000 to 8000 N. Therefore it is concluded that the maximum safe pay load for the given specification of the leaf spring is 7700N.

VI. TESTING OF LEAF SPRING

Static Test In the experimental analysis, the comparative testing of different steel leaf springs will help for drawing the conclusions. The steel and steel leaf springs are tested by using leaf spring test rig. The experimental set up is shown in

Fig 2. The leaf springs are tested by recommended standard procedure. The deflection or bending tests of selected spring for comparative study is taken on the universal testing machine.



A. Experiments setup

To conducted the load testing of leaf spring use of UTM (Universal Testing Machine) The experiment use following object to carried out successful analysis.

- 1) UTM
- 2) Height Gauge
- 3) Strain Gauge
- 4) Loading Movable support

Following figure show the two condition of test one before load applied and after load applied.

VII. CONCLUSION

From the practical and annoys result we concluded that we conducted test analyst the leaf spring on various load on specific time period.

Load (Newton)	Von-mises Stress N/mm^2			Bending Stress N/mm^2			Deflection mm		
	Theoretical	Practical	Ansys	Theoretical	Practical	Ansys	Theoretical	Practical	Ansys
1000	139.6	133	136.9	279.6	266.8	270.7	4.77	4.55	4.6
2000	282.6	178.5	280.7	558.2	555.8	556.8	9.54	8.85	9.15
3000	426.1	416.2	421.5	837.3	829.8	835.9	14.322	13.95	14.05
4000	568.8	557.8	562.7	1116.4	1108	1110.1	19.09	18.55	18.95
5000	712.6	698	698	1395.5	1387.4	1390.5	23.87	21.98	22.95
6000	852.3	839.2	838.7	1674.6	1665	1669.6	28.54	26.85	27.65
7000	993.5	978	977.8	1953.7	1947.9	1951.2	33.4	31.25	32.87
8000	1136.1	1129.5	1127.9	2332.5	2323.5	2328.4	38.192	36.02	37.95
9000	1277.6	1252.9	1250.9	2511.9	2509.9	2510.1	42.96	40.27	41.89
10000	1420	1399.5	1405.7	2791.6	2788.1	2790.2	47.74	44.93	46.85
11000	1458	1439.8	1742.1	3070.1	3061.8	3065.9	52.514	49.87	51.87
12000	1602.4	1588.9	1590.6	3349.2	3335	3345.44	57.28	55.5	55.98
13000	1746	1729	1729.4	3628.3	3617.5	3622.8	62.08	58.97	59.87
14000	1891.5	1878.5	1880.99	3907.4	3895.2	3905.8	66.83	63.58	65.12
15000	2037.1	2019.8	2026.77	4186.5	4178.2	4182.6	71.60	68.12	70.52

VIII. ACKNOWLEDGEMENT

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IX. REFERENCE

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