

Secure The Data using Modified Homomorphic Encryption and Paillier's Technique

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Abstract— Homomorphic Encryption is a Scheme which performs the operations on encrypted data. A homomorphic encryption scheme allows evaluating of encrypted data even without knowing the secret decryption key. It can be applied on various system by using different public key algorithms. The major advantage of the Homomorphic encryption can be taken by cloud computing applications. It supports the algebraic operations to be computed on the encrypted data. In this paper, the focus of homomorphic encryption scheme is based on the prime integers. This paper includes additive and multiplicative Homomorphism. Homomorphic encryption has wide range of applications like secured electronic voting system. The paper mainly focus on enhanced homomorphic encryption using paillier cryptography.

Keywords: Homomorphic Encryption, Security, Paillier's Technique

I. INTRODUCTION

With the evaluation of communication networks and digital communication, secure communication and data security is of paramount importance. Today one way to reach secure communication is by the use of cryptography. When the data is to be explored to the remote cloud server and the privacy of the sensitive data possible to attacks like un-trusted third party authentication computations, side channel attacks and implementation bugs in the system. Due to these attacks the homomorphic encryption is required to encrypt the computational data on server side. Thus a new idea of cryptosystem was proposed that allows the direct computation on the encrypted data. This concept is called "privacy homomorphism".

Then the concept of the privacy homomorphism[1] (homomorphic encryption) is introduced by the Rivest, Adleman and Dertouzos, which supports the computations on the encrypted data. While exclusively manipulating encrypted data, implicit additions multiplications on plaintext values can be performed by using the homomorphic encryption.

A. Homomorphism

Homomorphism is an algebraic term which refers mapping between the two groups (G, \square) and (H, \square) . Let (G, \square) and (H, \square) are two groups over some algebraic operation. A function $f: G \rightarrow H$ is called homomorphism.

B. Homomorphic Encryption

In 1978 Ronald Rivest, Elmore John Leonard Adleman and Michael Dertouzos advised for the primary time the construct of Homomorphic cryptography. Since then, very little progress has been created for thirty years. The cryptography system of Shafi Goldwasser and Silvio Micali was planned in 1982 was a demonstrable security cryptography theme that reached an interesting level of safety, it had been associate

additive Homomorphic cryptography, however it will code solely one bit. Within the same construct in 1999 Pascal Paillier was conjointly planned a demonstrable security cryptography system that was conjointly associate additive Homomorphic cryptography. Few years later, in 2005, Dan Boneh, Eu-Jin Goh and Kobi Nissim fictional a system of demonstrable security cryptography, with that we will perform a vast range of additives however only 1 multiplication.

Homomorphic encryption is the encryption is already encrypted data rather than on the original data with providing result as it is done on the plain text. The critical mathematical operations can be performed on the cipher text without changing the nature of the encryption.

C. Functions of Homomorphic Encryption

Homomorphic encryption is a set four functions as given below.

$H = \{\text{key Generation, Encryption, Evaluation, Decryption}\}$

- 1) Key Generation: client will generate pair of keys publickey pk and secret key sk for encryption of plaintext in this encryption.
- 2) Encryption: Using secret key sk client encrypt the plain text PT and generate $E_{sk}(PT)$ and along with public key pk this cipher text CT will be sent to the server.
- 3) Evaluation: A Server has a function f for doing evaluation of cipher text CT and performed this as per the required function using pk.
- 4) Decryption: Generated $Eval(f(PT))$ will be decrypted by client using its sk and it gets the original result. The following Diagram shows the Encryption and Decryption process.

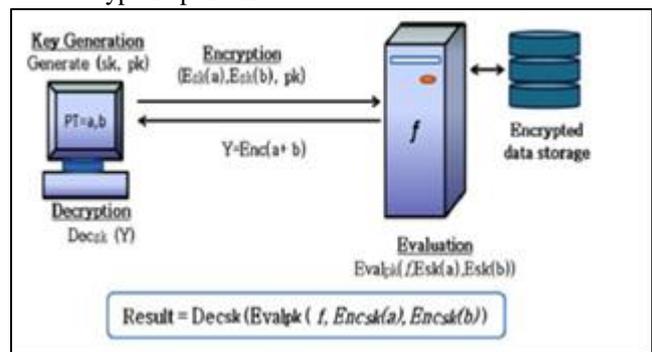


Fig. 1: Text Encryption and Decryption Process

D. Homomorphic Properties

The homomorphic encryption has two properties as stated below.

As the encryption functions is additively homomorphic, the following identities can be defined:

1) Homomorphic Addition of Plain Texts:

The product of 2 cipher texts will decrypt to the sum of their relative plaintexts. $D(E(m_1, r_1) \cdot E(m_2, r_2) \bmod n^2) = m_1 + m_2 \bmod n$.

2) Homomorphic Multiplication of Plain Texts:

The product of a cipher text with a plaintext raising will decrypt the sum of the related plaintexts, $D(E(m_1, r_1) \cdot gm^2 \bmod n^2) = m_1 + m_2 \bmod n$.

II. RELATED WORK

Payal V. Parmar[1] Security is the prime demand as a result of cybercrimes are increasing today. Today, the public setting is required to be secure for protective the protection of information. There are several personal environments are- offered however to store the information over those environments maybe valuable than public space. Hence, most are convenient to store the information on public cloud i.e. Internet. There are several encoding algorithms are offered [6]. Using those, the secure setting is created.

[6]. Using those, the secure setting is created. Homomorphic encoding allows that secure setting within which the operations will be done on the already encrypted information and therefore the same result may be obtained as on original information [7]. There are several homomorphic encoding schemes are delineate during this paper that makes use of this approach. Lets take an example of computation delogation where the user doesn't have the required resources to perform the computation on the data. In this article the user outsource his/her data to some service provider over the network or to the cloud. Now the user follows the following operation to perform the computation on his/her data. Pramod Kumar Siddharth[2] suggested the homomorphic properties of the cryptographic techniques take the attention of the scholars and makes it open research problem. The previous encryption schemes don't support the operations to be computed on the encrypted data, which may compromise the privacy of the sensitive data. The homomorphic encryption supports the mathematical operations to be computed on the encrypted data. This algebraic property of the homomorphic encryption scheme have a wide application areas such as secure electronic voting, multiparty computation, private searching, delegation of computation and many more. In this article we proposed a homomorphic encryption scheme based on the Carmichael's theorem over integers. The operations in the operations are modular arithmetic. The paper also discuss the security scheme and further optimization are pointed out.

Tannishk Sharma [3] suggested an efficient E-voting system in his article as fallows. A traditional voting system can be time consuming and cumbersome and takes a lot of time. With the growing development of Information Technology an E voting system tends to overcome all these limitations. E- voting is fast and helps us to cast our vote from any location. One of the main focus of then E-Voting System is security. In this paper he proposed an E-Voting System using Paillier Homomorphic Encryption Scheme which is used to provide security to the voting system and in turn help us to modify and transfer data in the encrypted form making it impenetrable. Here he uses the Paillier Encryption

Homomorphic property that allows us to add the votes in encrypted form. The online vote casting system is more reliable than the traditional system and is able to save the time

III. PROPOSED SYSTEM

The Paillier Cryptography is a modular, public key encryption scheme, created by Pascal Paillier, with many interesting properties. This paper will explore the improved or enhanced Paillier's work by concatenating the concept of the cryptographic Thresholding, Which distributes the process amongst a number of parties such that a message can only be decrypted if a certain qualified subset of these parties participates in the decryption method. The cryptosystem that supports such a process is called a threshold cryptosystem. It is assumed that the reader is familiar, to some degree, with modular arithmetic, as well as the concept of converting an alphanumeric message into a purely numeric message. Also, the term plaintext will be used to refer to a message that is numeric, but is not encrypted, while the term cipher text will be used to refer to plaintexts which have been encrypted, but not yet decrypted. In order to illustrate the system's potential. We will initiate with the encryption process with the combination of the blowfish algorithm to output the encrypted stream called the cipher text. It takes a variable-length key from 32 bits to 448 bits which makes it more feasible than other encrypting algorithms maintain its reliability and superiority parameters.

No attack is known to be successful against it. Since the security algorithms performance along with malleability forms a mandatory criterion. Since there doesn't exist yet known concept on the Paillier's algorithms that confronts the malleability and performance concept and makes the concept stupendous. Hence in supporting the idea we try to bring out a novel system that takes into measures both of two parameters.

The Proposed methodology is homomorphic encryption based on paillier encryption cryptography. The proposed scheme is stated below.

A. Paillier Cryptosystem (1999):

The Paillier theme, was fictional by Pascal Paillier in 1999 it's a probabilistic theme that's homomorphic with relevance addition (the add of 2 ciphertext is capable the ciphertext of the add of the 2 plaintext equivalents) and to multiplication by a relentless. Paillier could be a form of keypair-based cryptography. This suggests every user gets a public and a personal key, and messages encrypted with their public key will solely be decrypted with their personal key.

Suppose E is that the paillier secret writing performs then we've the subsequent 2 properties:

$$E(a)+E(b) = E(a+b)$$

$$E(a)^b = E(a * b)$$

Paillier consists of 3 algorithms actually 3 algorithms area unit necessary to form associate secret writing theme. First you would like a Key generation algorithmic rule, second associate secret writing algorithmic rule and last a decipherment algorithmic rule let's see however Paillier implement those Key Generation. To generate a key you decide on 2 large primes p and Q

specified: $\gcd(pq, (p-1)(q-1)) = 1$. In other words the merchandise of p and Q and $(p-1)$ and $(q-1)$ are unit comparatively prime (their greatest common factor is 1).

Then you reckon 2 parameters n & λ specified: $n = pq$ and $\lambda = \text{lcm}(p-1, q-1)$ lowest common multiple is that the least integer for instance $\text{lcm}(4, 8) = 16$. Select a random number g like g belongs to the set of integers modulo n square. During this case (p and Q are unit primes of an equivalent length) you'll choose g as $n+1$. Compute alphabetic character like alphabetic character = $\lambda^{-1} \pmod n$ (modular increasing inverse).

The public key's (n, g) and therefore the personal key's (λ, μ) Encryption.

Suppose m and r is random number such as:

$$m < n \text{ and } r < n$$

$$c = g^m * r^n \pmod{n^2}$$

c is the ciphertext of m

Decryption

$$M = L(c^\lambda \pmod{n^2}) * \mu \pmod n$$

$$L(x) = (x-1) / n$$

Example with small parameters and proof of homomorphism

let $p = 11$ and $q = 13$

$$n = pq = 143$$

$$g = n+1 = 144$$

The public key is (143, 144)

$$m = 50$$

we pick $r : r = 23$

$$c = g^m * r^n \pmod{n^2}$$

$$= 144^{50} * 23^{143} \pmod{143^2} = 9637$$

$$m = L(c^\lambda \pmod{n^2}) * \mu \pmod n$$

$$\lambda = (p-1) * (q-1) = 20 * 12 = 240 \quad \mu = \lambda^{-1} \pmod n$$

$$n = 120^{-1} \pmod{143}$$

$$m = L(9637^{120} \pmod{143^2}) * (120^{-1} \pmod{143}) \pmod{143}$$

$$m = 50$$

Now that we have a tendency to outlined the the procedure to get a key pair, code and decode let's discuss the homomorphic properties of Paillier.

1) Addition:

The product of 2 ciphertexts decrypts to their total, if i need to try and do addition on ciphertexts comparatively to my plaintexts I even have to calculate the merchandise of the ciphers

Proof suppose E is that the encoding formula and money supply and money supply the plaintexts: $E(m1) * E(m2) = (g^{m1} * r1^n)(g^{m2} * r2^n) \pmod{n^2} = g^{(m1+m2)} (r1r2)^n \pmod{n^2} = E(m1+m2)$

2) Multiplication:

If I even have a plaintext m and a continuing k then the encoding of their product evaluates to the cipher of m raised to the facility k .

Proof same suppositions regarding $E, m1, m2$ as before: $E(m1)^k = (g^{m1} * r1^n)^k \pmod{n^2} = g^{(m1k)} (r1^n)^k \pmod{n^2} = E(m1k)$

3) Algorithm

1) Step 1: Process of Key Generation takes place by using following

Produce two large prime numbers a and b randomly which are independent of each other such that $\gcd(a*b, (a-1)*(b-1)) = 1$.

Calculate $n = ab$ and $k(n) = \text{lcm}(p-1, q-1)$ where $k(n)$ being Carmichael function.

Select the generator g such that g belongs to \mathbb{Z}_n^2

Compute the follow Modular Multiplicative inverse $u = (L(g \pmod{n^2}) - 1) \pmod n$ where $L(u) = (u-1)/u$ So Pair of Key Generated: the public key is (n, g) and the private key is (k, u).

2) Step 2: Encryption Process

1) The message m is need to be encrypted where m belongs to \mathbb{Z}

2) Choose a random number r

3) Compute cipher text $c = gm * rn \pmod{n^2}$

3) Step 3: Decryption Process

1) Cipher text c will be decrypted to get message m as follows by using private key (k, u): $m = L(c^k \pmod{n^2}) * u \pmod n$

IV. RESULTS AND ANALYSIS

Key generation

Number of bits

public n: -

private lambda: -

Elapsed time (keygen): - ms

A. Key Generation

Key generation

Number of bits

public n:

937603166561331534071430487590445852596360473197663783141818687823896540805336786
93983233114906724537067174495523286250857511928284231005661222215964632596951031
798263307326549803732171878508491609724413709281814982453186867461642897443152224
19439291860699395987088958735938900993631221024038203107194083071

private lambda:

156267194426888589011905081265074308766060078866277297190303114637316090134222797
823305388524844540895111957492538810418095853213807051676102037035994105399315829
703173309565468236747218738347651827460489522946889721659911259692161478170122422
71635215892318435880141225217481926367931331104130210287446795072

Input values

Value A:

Value B:

[A] = -

Elapsed time: - ms

[B] = -

B. Encrypting the input values

Input values

Value A:

Value B:

[A] = -

Elapsed time: - ms

[B] = -

C. Decrypting the message and getting the results

Input values

Value A: 20
Value B: 60 [Encrypt]

[A] =
216880482497580122605788286848973065837540415450154890660797071968322555637607128
560120719859162990561159860832256815001115251248876982038307395099990934036221397
460831040927730926507748499875525147106445340496361567171819173438678373217502428
778086814247325417689649653381469420748652849652139969489760054832847761328419323
24640728463499284056841148169612045225809880638278313813474601023833739665418635
609641233561650954053948139541759782268228315904636031994584950171611523491586622
733360423008899447097308839494716823265997652919991189222958330705029118248600072
7277382293010984884474719263235110384967076912994

Value C: 5
[Calculate ((A+B)*C)]

[(A + B)*C] =
717843397482498037222004526756247471937498396206373069667386360082315863349920798
417182023849266723285552845280410159505634329842864893485036735610686564002355050
48363323497113080477228595243795718512497213280649484257594554575691897317174279
213367429956419829744364501563084827244596095661150035636564622704750618628509549
420818920801061590351779170221454716995780177000279309127058159145213035876959779
45084556368942866505778568923219008792449317378288216756234487686142440214214464
920101012104512105318052970487380295995877342728091385304983142408827182131696171
6672611382944644397099484004758160491483672537082

Elapsed time: 0 ms

Decryption

[Decrypt]

(A + B)*C = 400

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V. CONCLUSION

Security or privacy on fully Homomorphic encryption is a traditional concept on security which enables us to provide the encrypted data without knowing the prime entries on which the calculation was carried out respecting the confidentiality of data. However, our work is depends on the application of Homomorphic encryption which enables us to derive the security of the data and also its performance issue. As it is evaluated in the graphs of the malleability and performance it is evident that our algorithm provides a novel result which is found to be good making the security of the Paillier's algorithm much compact and flexible. And Finally This paper carried out the Enhanced performance of Homomorphic Encryption based on paillier's cryptography.

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